

# Plasmons, Plasmons Polaritons de Surface et application en Nanoptique

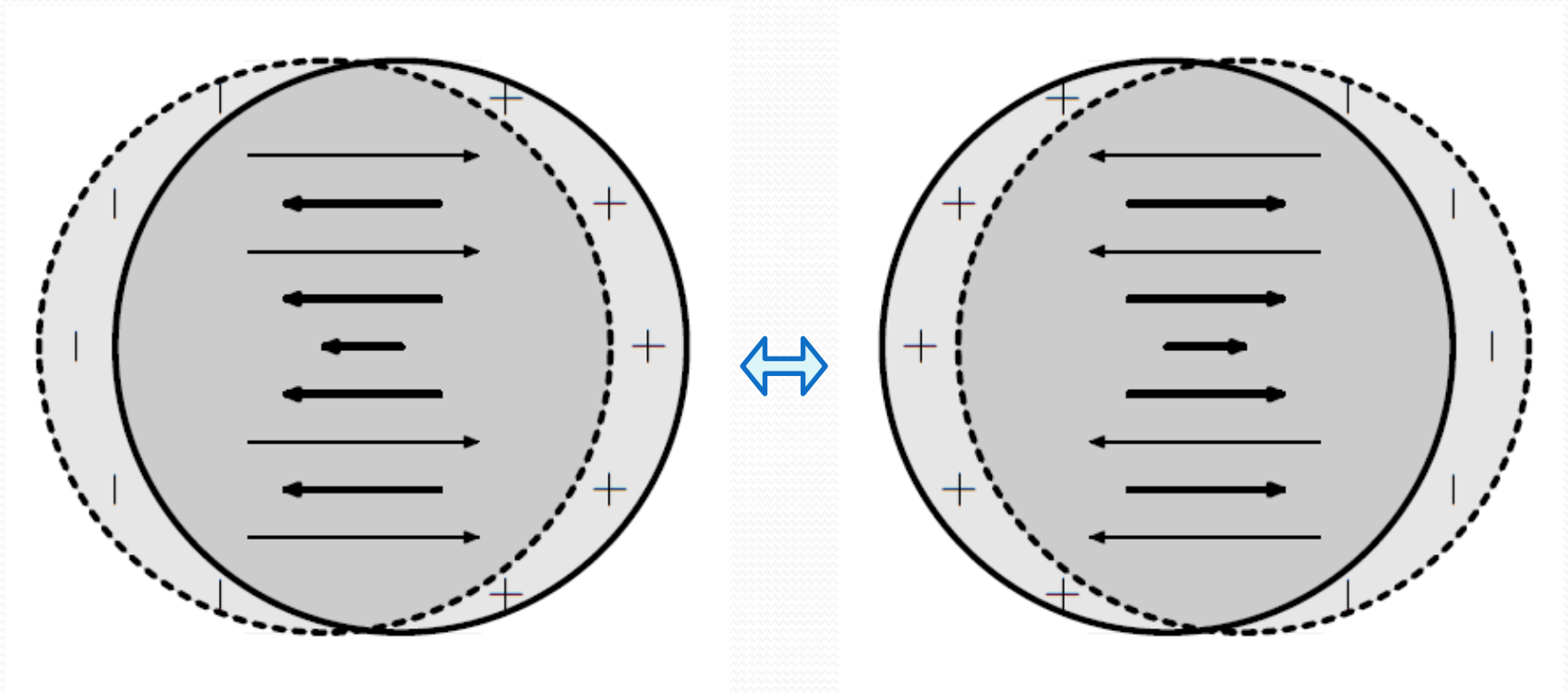
Physique de la matière condensée et nano-objets

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# Plasmons

- Quantum d'oscillation du plasma  
(oscillation de densité de charges libres)



- Excitation collective

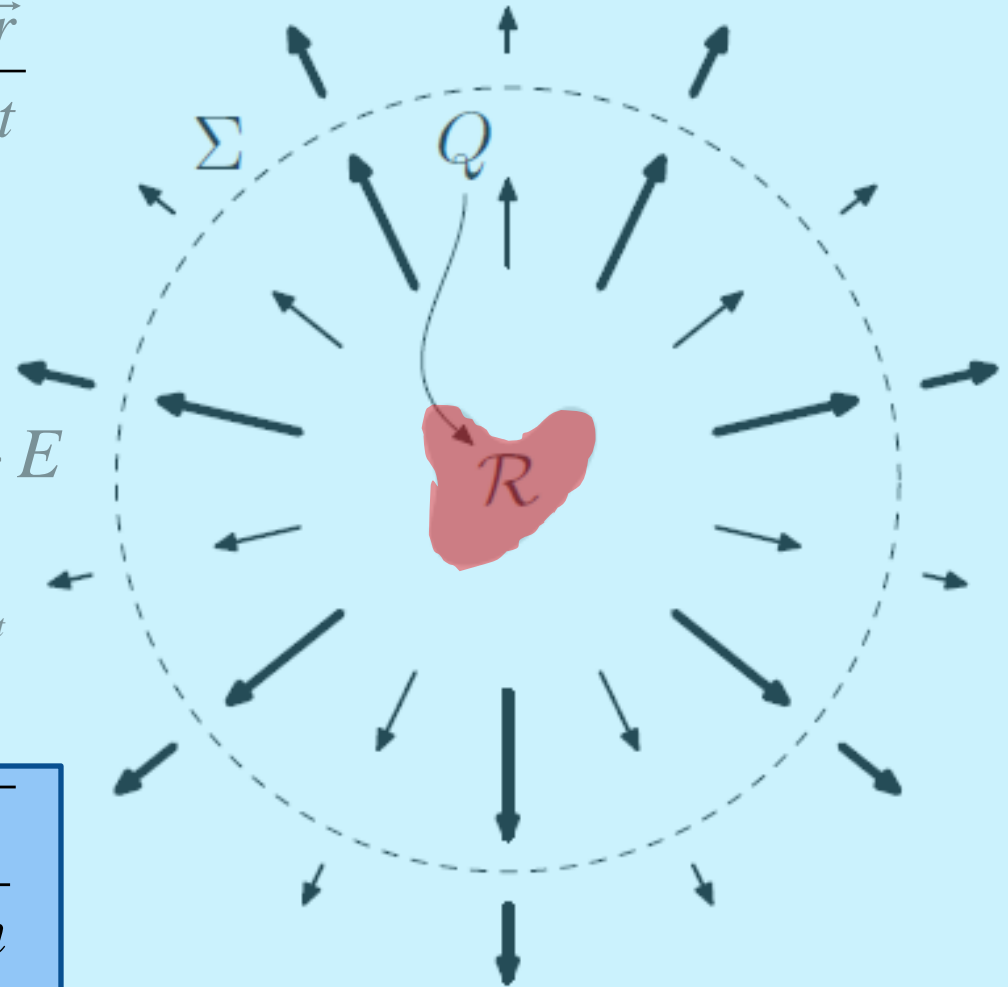
# Fréquence Plasma

$$m \frac{d^2 \vec{r}}{dt^2} = -eE(\vec{r}, t) \quad \vec{j} = -n_0 e \frac{d\vec{r}}{dt}$$

$$\frac{\partial \vec{j}(\vec{r}, t)}{\partial t} = \left( \frac{n_0 e^2}{m} \right) E(\vec{r}, t)$$

$$\frac{d}{dt} \int_{\Sigma} d\vec{a} \cdot \vec{j}(\vec{r}, t) = \left( \frac{n_0 e^2}{m} \right) \int_{\Sigma} d\vec{a} \cdot E$$

$$\frac{d^2 Q}{dt^2} = -\frac{4\pi n e^2}{m} Q \quad Q = Q_0 e^{-i\omega_p t}$$



CGS

$$\omega_p = \sqrt{\frac{4\pi n e^2}{m}}$$

SI

$$\omega_p = \sqrt{\frac{n e^2}{\epsilon_0 m}}$$

$$E_p = \hbar \omega_p \approx 5 - 15 \text{ eV}$$

# Permittivité diélectrique

$$\epsilon(\omega, \vec{k})$$

$$m \frac{d^2 \vec{r}}{dt^2} = -e \vec{E}$$

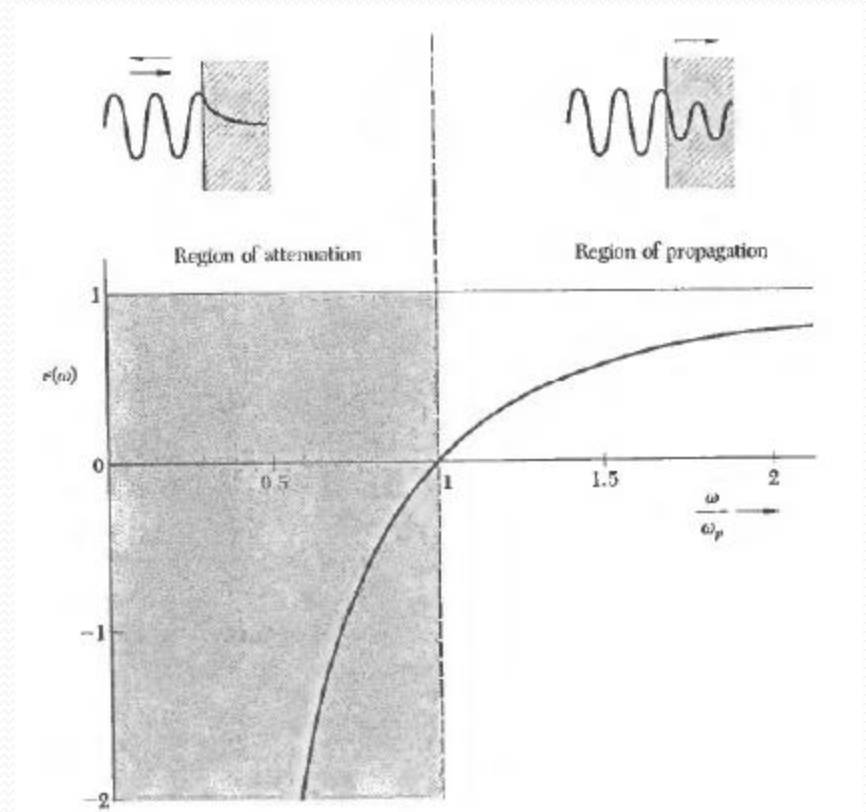
$$E \propto e^{-i\omega t}$$

$$\vec{r} = \frac{e}{m\omega^2} \vec{E}$$

$$\vec{P} = -n_0 e \vec{r} = -\frac{ne^2}{m\omega} \vec{E}$$

$$\epsilon(\omega) = \frac{D(\omega)}{E(\omega)} = 1 + 4\pi \frac{P(\omega)}{E(\omega)} = 1 - \frac{4\pi ne^2}{m\omega^2}$$

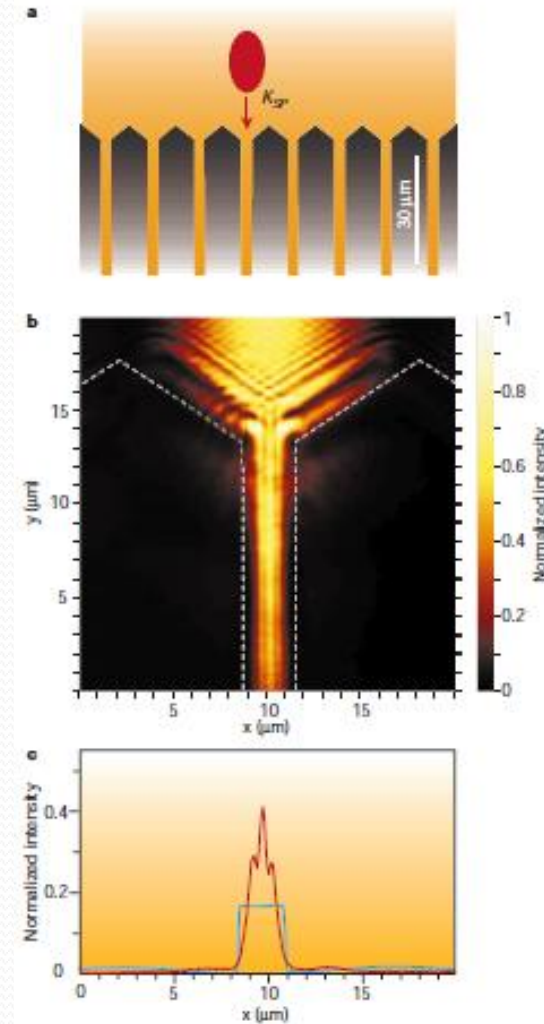
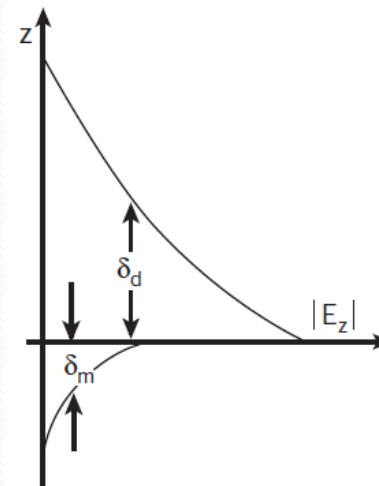
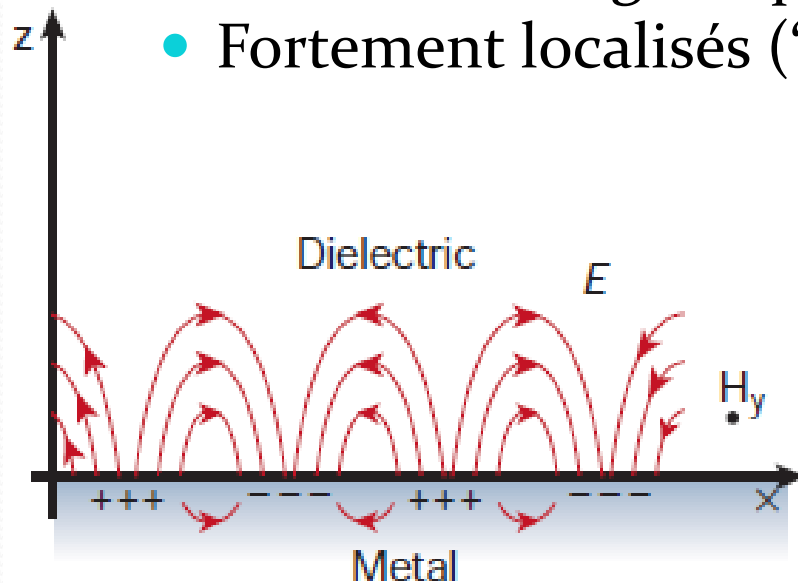
$$\epsilon(\omega) = 1 - \frac{\omega_p^2}{\omega^2}$$



# Plasmon Polaritons de Surface

## Plasmons de Surface

- Transverse magnétiques
- Fortement localisés (“évanescents”)



## Plasmon Polaritons

- Couplage photon – plasmon
- propagation jusqu'au mm

# Relation de dispersion - Volume

Ondes électromagnétiques dans un gaz d'électrons libres

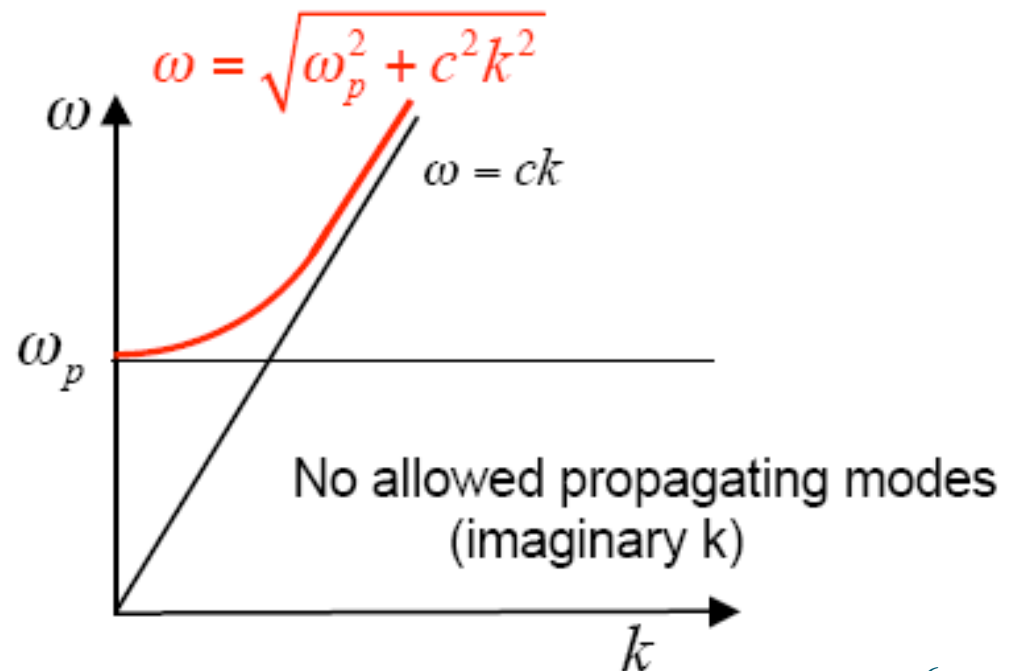
$$\frac{\partial^2 \vec{D}}{\partial t^2} = c^2 \nabla^2 \vec{E}$$

Equation d'onde

$$\vec{E} \propto e^{-i\omega t} e^{i\vec{k} \cdot \vec{r}}$$

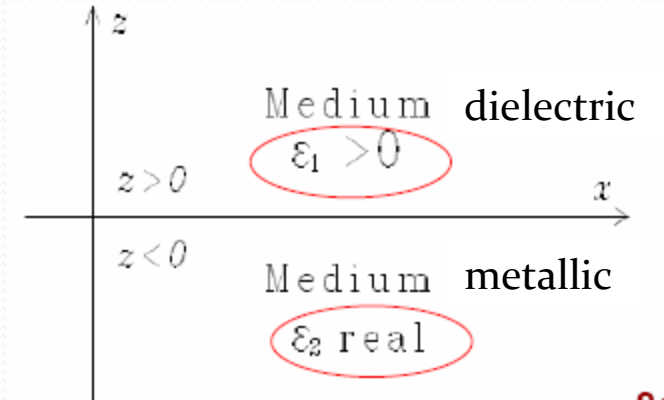
$$\epsilon(\omega, \vec{k}) \omega^2 = c^2 k^2$$

$$\omega^2 - \omega_p^2 = c^2 k^2$$



# Relation de dispersion – SPs – 1

$$\begin{aligned}
 z < 0 & \begin{cases} \mathbf{H}_d = (0, H_{yd}, 0) \exp i(k_{xd}x + k_{zd}z - \omega t) \\ \mathbf{E}_d = (E_{xd}, 0, E_{zd}) \exp i(k_{xd}x + k_{zd}z - \omega t) \end{cases} \\
 z > 0 & \begin{cases} \mathbf{H}_m = (0, H_{ym}, 0) \exp i(k_{xm}x + k_{zm}z - \omega t) \\ \mathbf{E}_m = (E_{xm}, 0, E_{zm}) \exp i(k_{xm}x + k_{zm}z - \omega t) \end{cases}
 \end{aligned}$$



Dans le moyen i :

$$\nabla \times \vec{H}_i = \epsilon_i \frac{d\vec{E}_i}{dt} \quad \Rightarrow \quad \left( k_{zi} H_{yi}, 0, i k_{xi} H_{yi} \right) = \left( \omega \epsilon_i E_{xi}, 0, i \omega \epsilon_i E_{zi} \right)$$

$$k_{zi} H_{yi} = -\omega \epsilon_i E_{xi} \quad \left\{ \begin{array}{l} k_{zm} H_{ym} = -\omega \epsilon_m E_{xm} \\ k_{zd} H_{yd} = -\omega \epsilon_d E_{xd} \end{array} \right.$$

Continuité à la surface

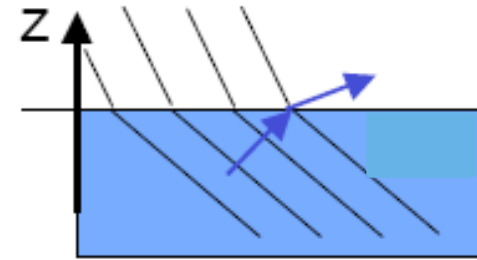
$$\left\{ \begin{array}{l} E_{xm} = E_{xd} \\ H_{ym} = H_{yd} \end{array} \right.$$

$$\frac{k_{zm}}{\epsilon_m} = \frac{k_{zd}}{\epsilon_d}$$

# Relation de dispersion – SPs – 2

Pour toutes les surfaces :

$$k_{xm} = k_{xd}$$



Si on suppose que  $\mu=1$  et  $k_y=0$

$$|k| = \frac{n\omega}{c}$$

$$k_x^2 + k_{zi}^2 = \epsilon_i \left( \frac{\omega}{c} \right)^2$$

$$\left. \begin{aligned} k_{sp} = k_x &= \sqrt{\epsilon_i \left( \frac{\omega}{c} \right)^2 - k_{zi}^2} \\ \frac{k_{zm}}{\epsilon_m} &= \frac{k_{zd}}{\epsilon_d} \end{aligned} \right\}$$

$$k_{sp} = \frac{\omega}{c} \sqrt{\frac{\epsilon_d \epsilon_m}{\epsilon_d + \epsilon_m}}$$

**Relation de dispersion des plasmons surfaciques**

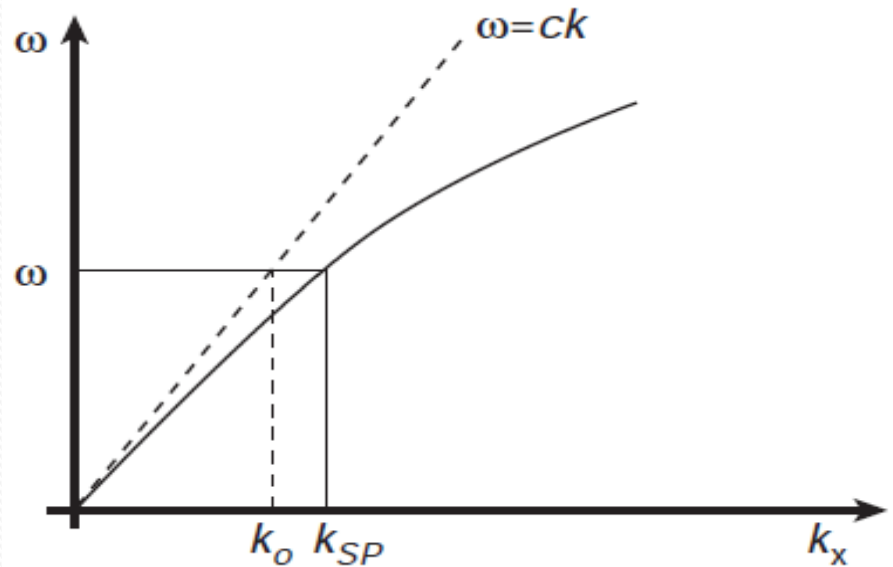


# Couplage photon-plasmon

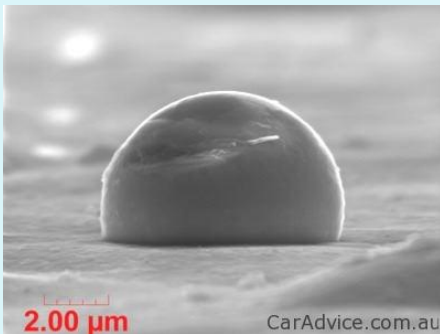
- Différent moment:

$$\hbar k_{sp} \neq \hbar k_0$$

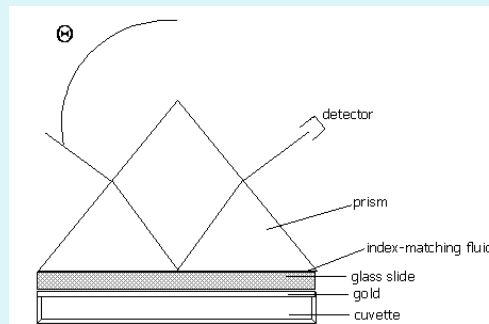
$$k_{sp} = k_0 \sqrt{\frac{\epsilon_d \epsilon_m}{\epsilon_d + \epsilon_m}}$$



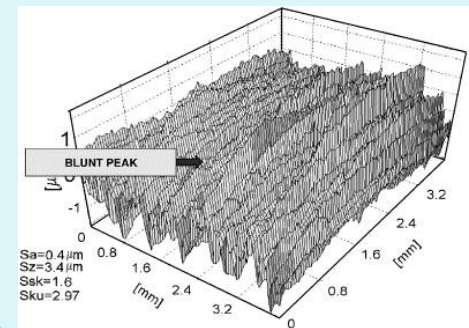
diffusion par un défaut



couplage avec prismes

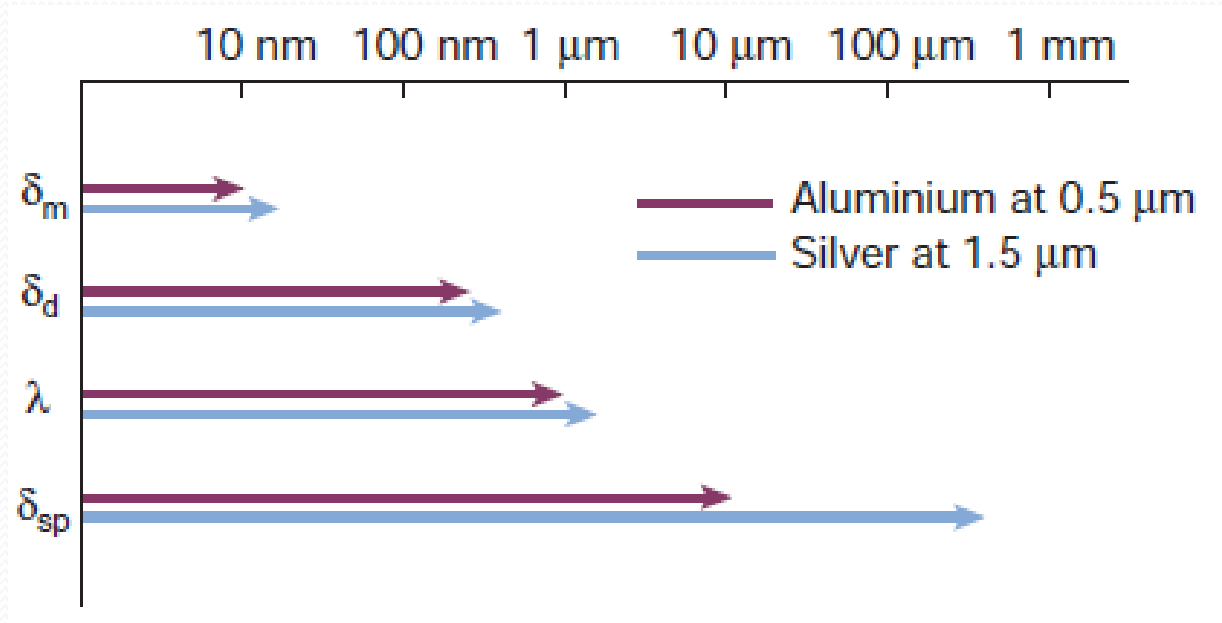


rugosité périodique



# Couplage photon-plasmon

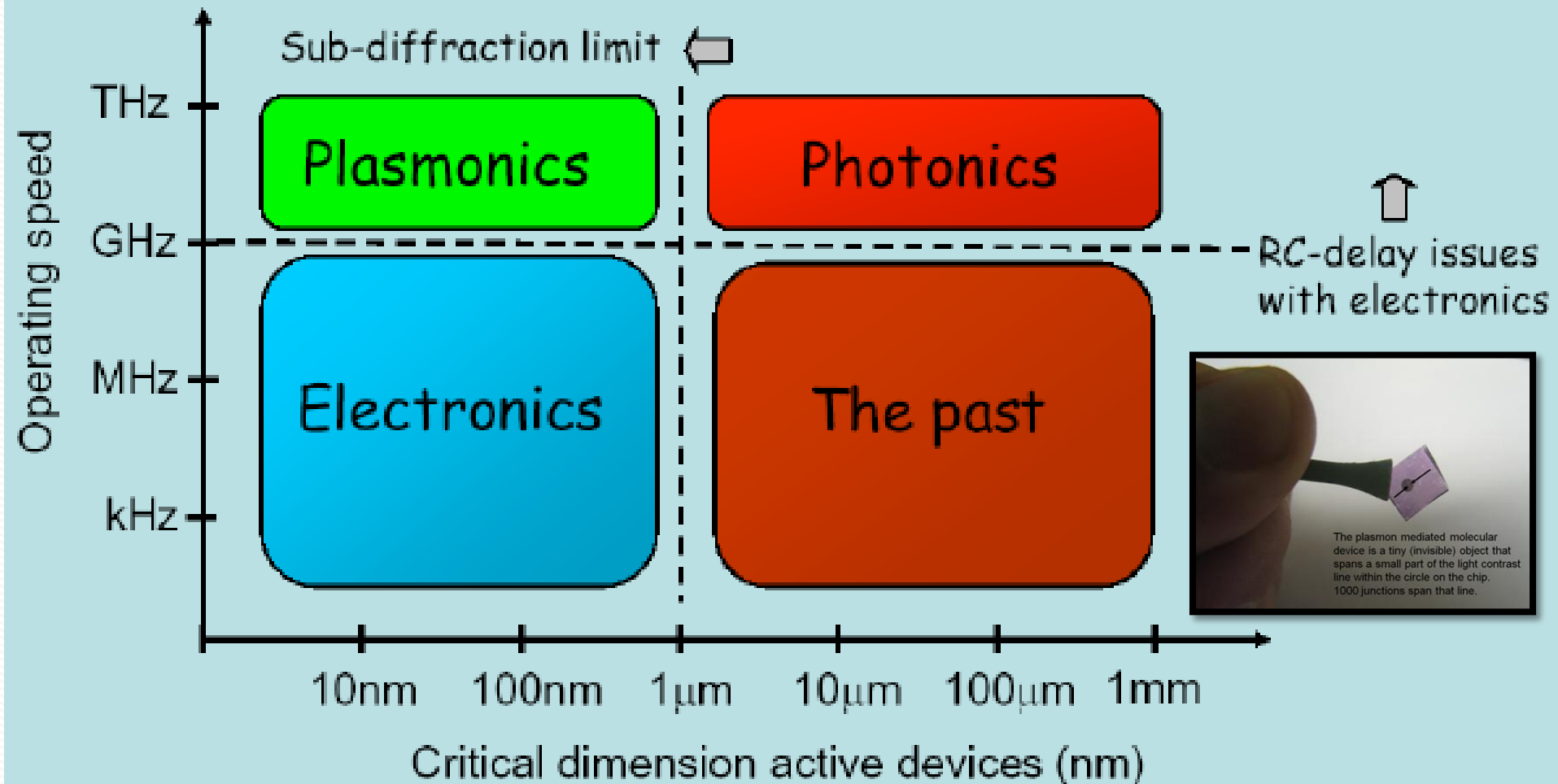
- Décadence exponentielle perpendiculairement à la surface



- Atténuation par absorption dans le métal

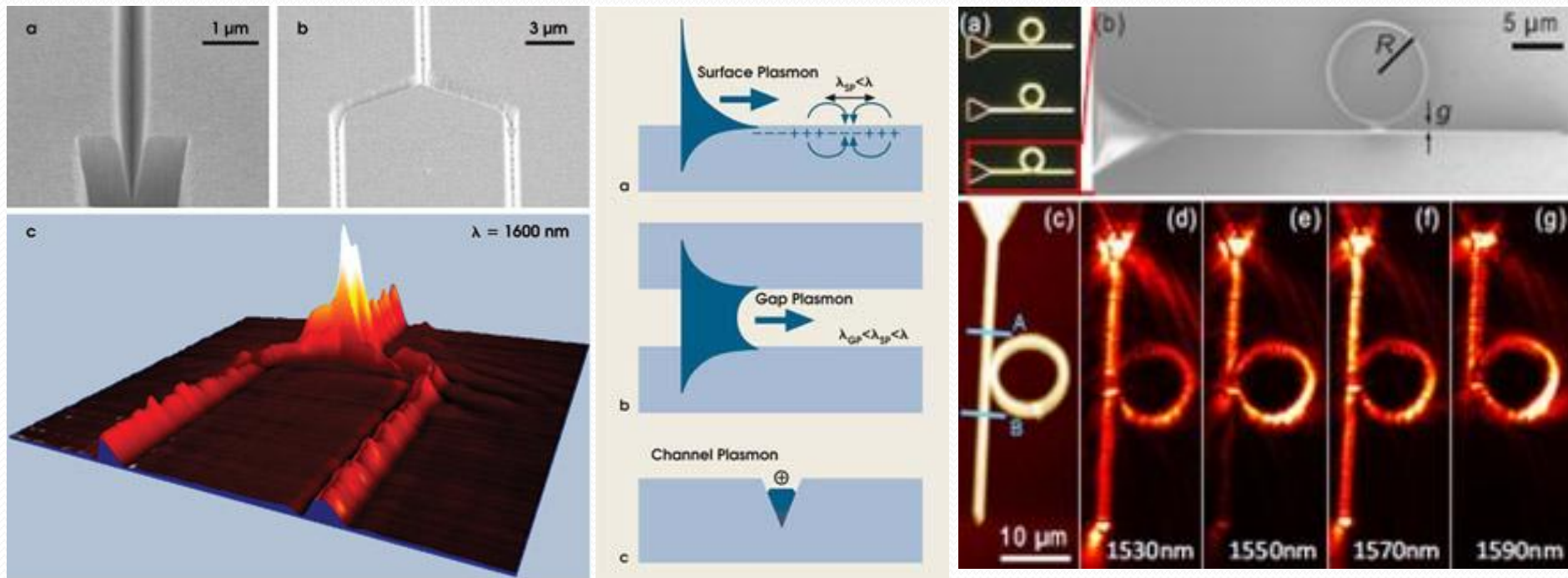
$$\delta_{SP} = \frac{1}{2k''_{SP}} = \frac{c}{\omega} \left( \frac{\epsilon'_m + \epsilon_d}{\epsilon'_m \epsilon_d} \right)^{\frac{3}{2}} \frac{(\epsilon'_m)^2}{\epsilon''_m}$$

# Nanocircuits



# Nanocircuits

## Channeling Surface Plasmons

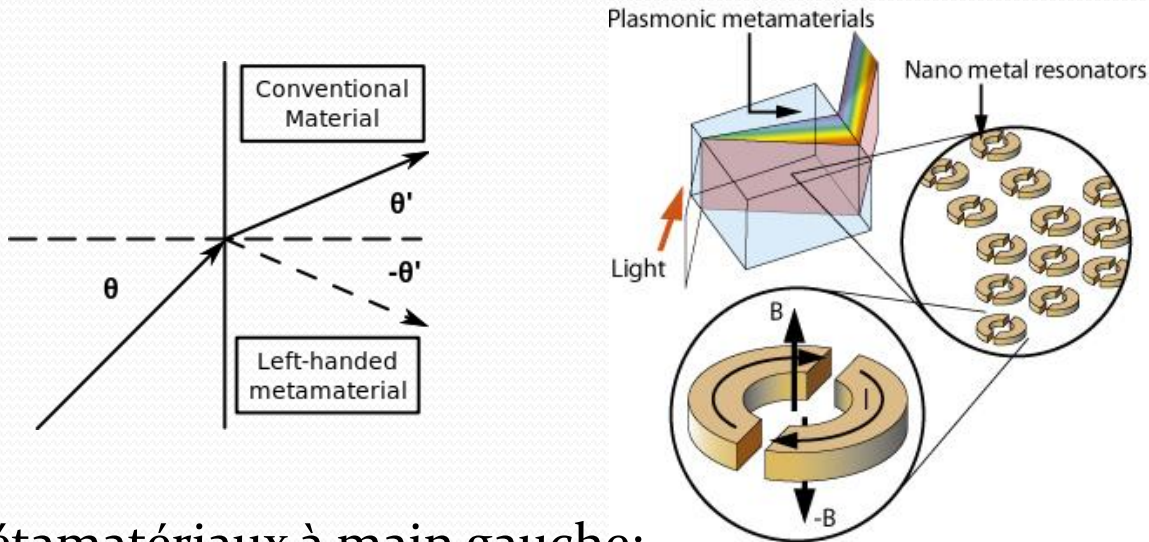


Microscope optique en champ proche (NSOM)

# Métamatériaux plasmoniques

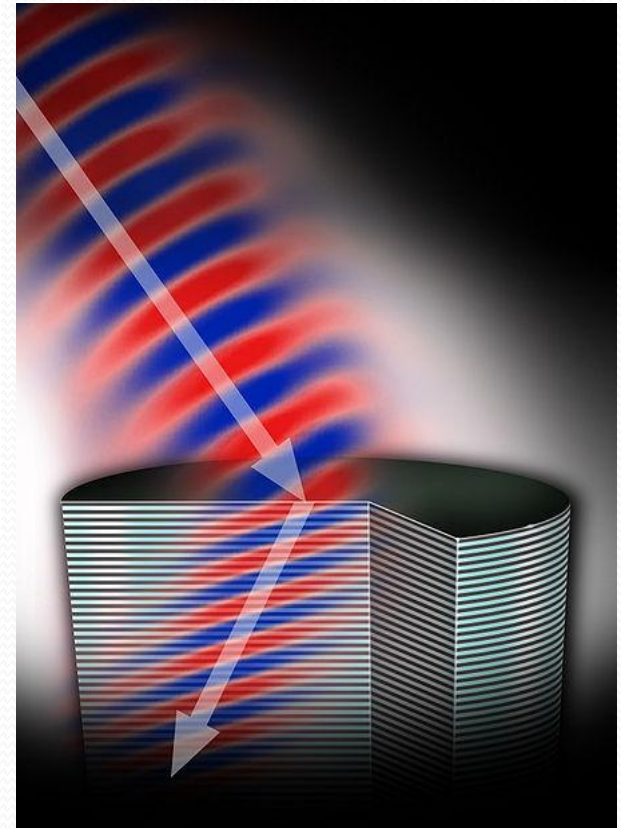
## Métamatériaux:

matériaux avec propriétés électromagnétiques qui n'existent pas en nature



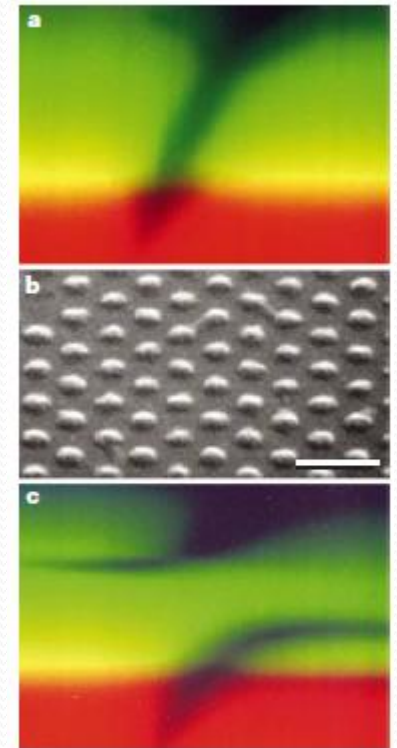
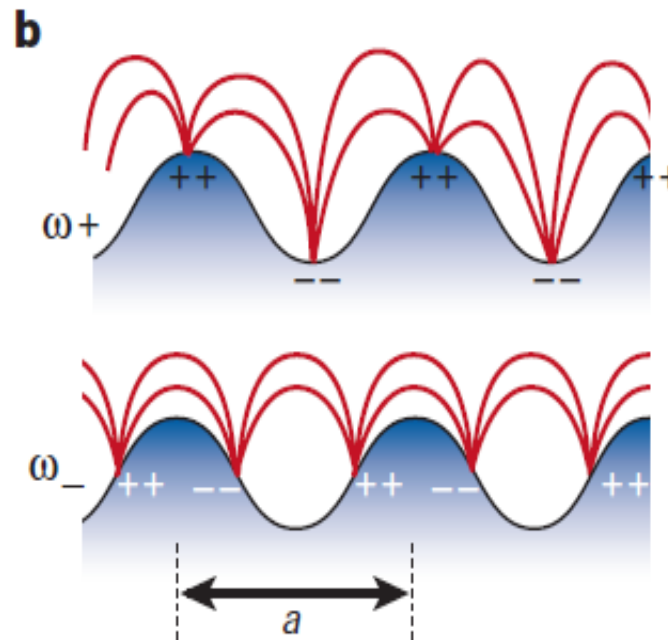
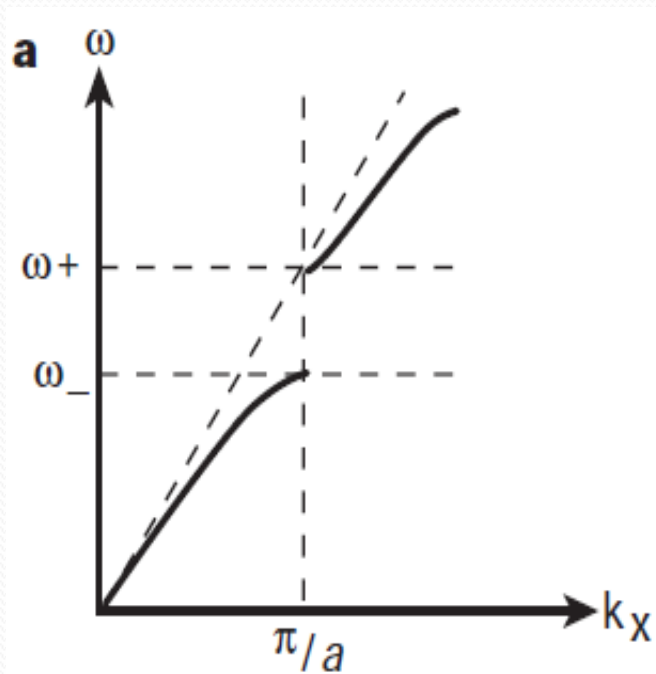
## Métamatériaux à main gauche:

- indice de réfraction négatif
- vitesse de phase et groupe opposées
- effet Doppler inversé
- effet Tcherenkov inversé



# Métamatériaux plasmoniques

Métamatériaux à bandes photonique (PBG) - à SPs bandes

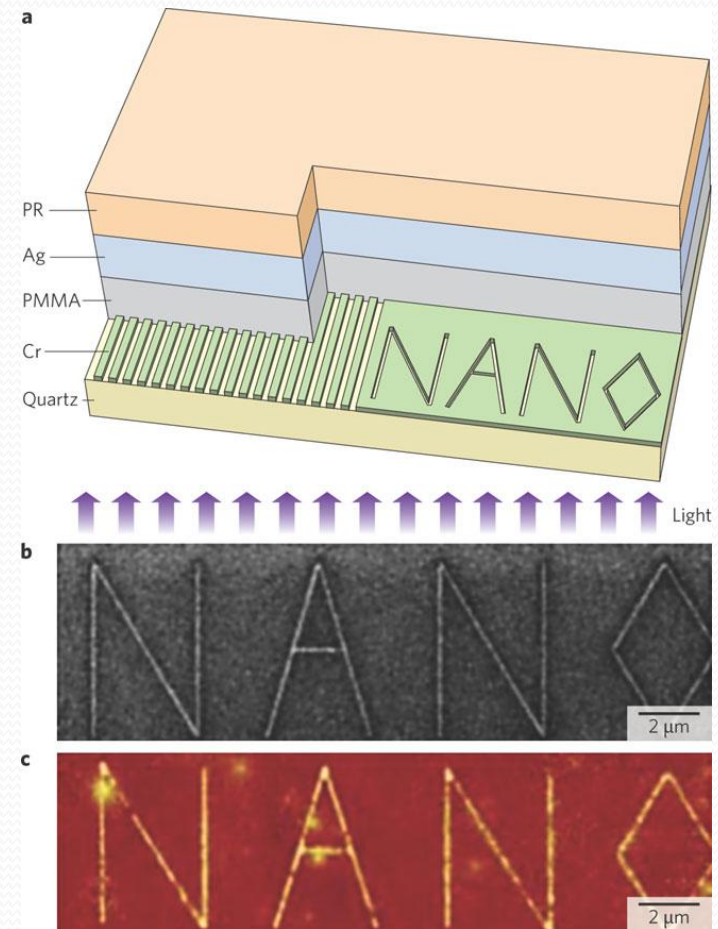
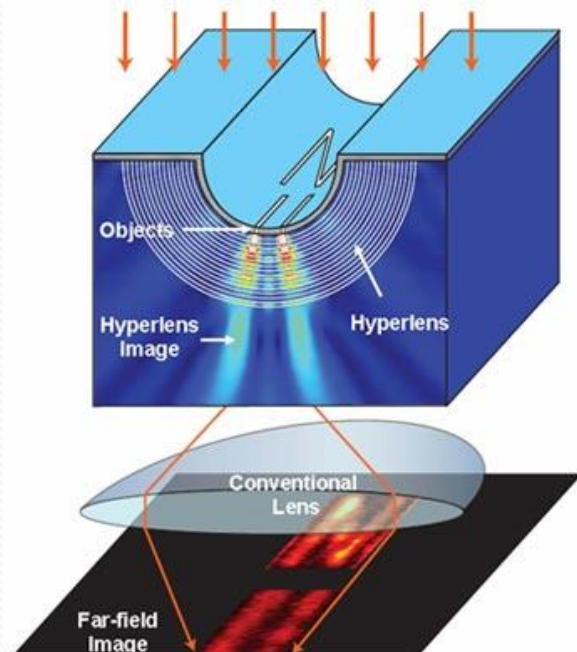




# Métamatériaux plasmoniques

## Images sous longueur d'onde (subwavelength imaging)

voir structures plus petites de la longueur d'onde de la lumière visible par moyen des images optiques



→ Superlentille

# Transmission optique extraordinaire

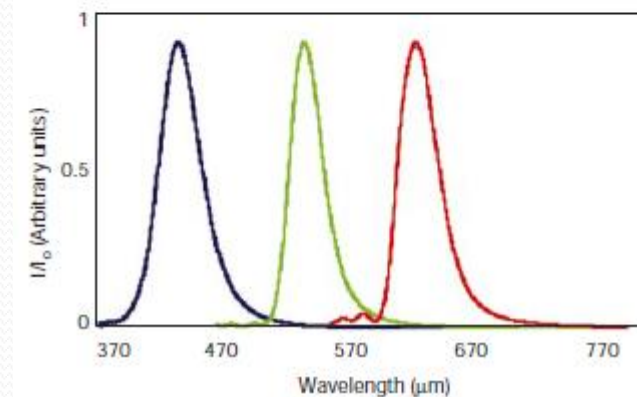
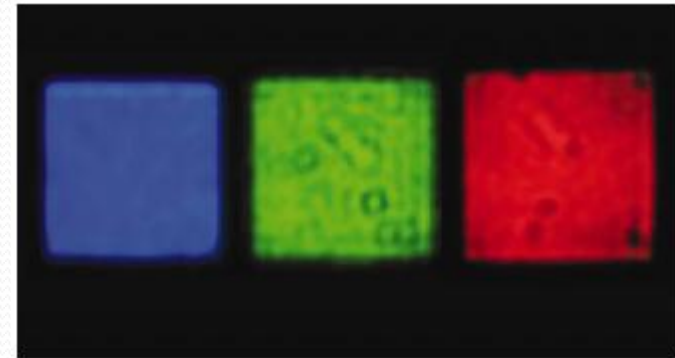
**EOT:** amélioration de la transmission de la lumière par moyen d'ouvertures (trous) de dimensions inférieure à la longueur d'onde et périodiques.

Modulation des propriétés :

- dimensions
- distances

Effets de:

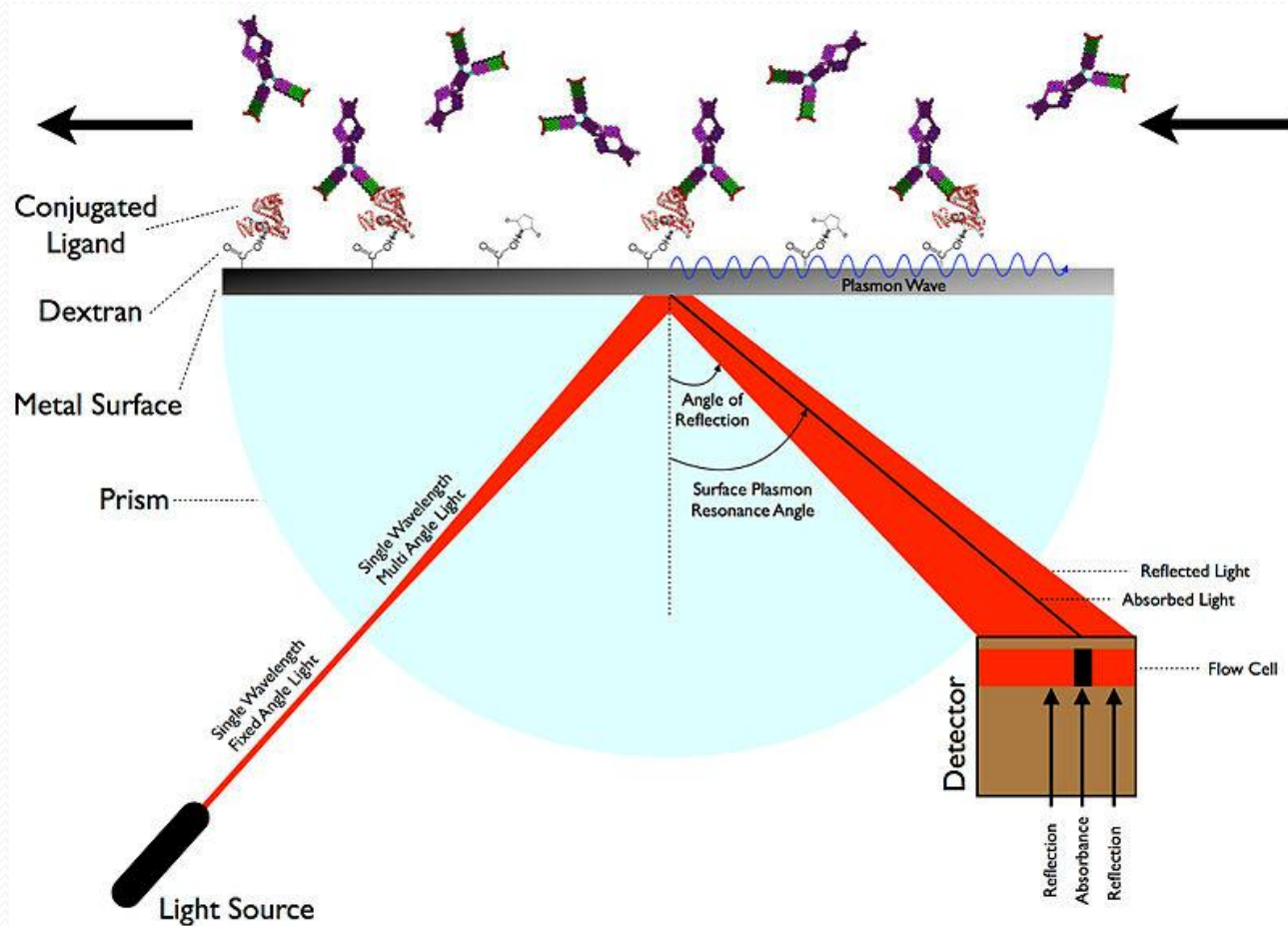
- tunneling
- résonance





# Résonance des plasmons de surface

**SPR:** oscillation collective des électrons de valence d'un solide stimulé par lumière incident avec fréquence correspondant à la fréquence plasma

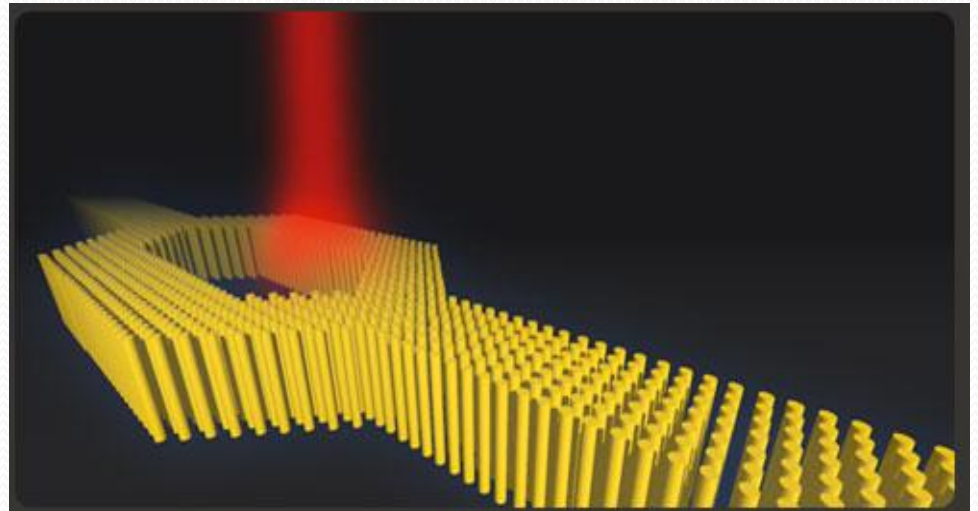


# Conclusions

Développements futurs:

- réutilisation d'une partie de l'énergie des OLED
- composants photoniques non linéaires
- nouvelles technologies dans les domaines sous longueur d'onde
- Spinning-plasmonics

*Merci pour votre attention*



# Bibliographie

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